

# STATICS AND MECHANICS OF MATERIALS

Sixth Edition



R. C. HIBBELER

# STATICS AND MECHANICS OF MATERIALS

SIXTH EDITION

*This page intentionally left blank*

# STATICS AND MECHANICS OF MATERIALS

SIXTH EDITION

R. C. HIBBELER



Content Management: Erin Ault  
Content Production: Rose Kernan, Sandra Rodriguez, Prerna Rochlani, Scott Disanno, Pallavi Pandit  
Product Management: Holly Stark  
Product Marketing: Krista Clark  
Rights and Permissions: Tanvi Bhatia/Anjali Singh  
Cover Image: Jess Kraft/Shutterstock

Please contact <https://support.pearson.com/getsupport/s/> with any queries on this content.

**Copyright © 2024, 2017, 2014 by R. C. Hibbeler. Published by Pearson Education, Inc. or its affiliates, 221 River Street, Hoboken, NJ 07030.** All Rights Reserved. Manufactured in the United States of America. This publication is protected by copyright, and permission should be obtained from the publisher prior to any prohibited reproduction, storage in a retrieval system, or transmission in any form or by any means, electronic, mechanical, photocopying, recording, or otherwise. For information regarding permissions, request forms, and the appropriate contacts within the Pearson Education Global Rights and Permissions department, please visit [www.pearsoned.com/permissions/](http://www.pearsoned.com/permissions/).

Acknowledgments of third-party content appear on page xxvii, which constitutes an extension of this copyright page.

PEARSON, ALWAYS LEARNING, and Mastering are exclusive trademarks owned by Pearson Education, Inc. or its affiliates in the U.S. and/or other countries.

Unless otherwise indicated herein, any third-party trademarks, logos, or icons that may appear in this work are the property of their respective owners, and any references to third-party trademarks, logos, icons, or other trade dress are for demonstrative or descriptive purposes only. Such references are not intended to imply any sponsorship, endorsement, authorization, or promotion of Pearson's products by the owners of such marks, or any relationship between the owner and Pearson Education, Inc., or its affiliates, authors, licensees, or distributors.

#### **Library of Congress Cataloging-in-Publication Data**

Names: Hibbeler, R. C., author.

Title: Statics and mechanics of materials / Russell C. Hibbeler.

Description: Sixth edition. | Hoboken, NJ : Pearson, [2023] | Includes index. | Summary: "This book is a combined abridged version of Engineering Mechanics: Statics and Mechanics of Materials. It provides a clear and precise presentation of the fundamental topics of both these subjects" — Provided by publisher.

Identifiers: LCCN 2022037453 | ISBN 9780137964895 (hardcover) | ISBN 9780137964932 (ebook)

Subjects: LCSH: Strength of materials. | Statics. | Structural analysis (Engineering)

Classification: LCC TA405 .H48 2023 | DDC 620.1/12—dc23/eng/20221004  
LC record available at <https://lccn.loc.gov/2022037453>

#### **ScoutAutomatedPrintCode**



Rental  
ISBN-10: 0-13-796489-7  
ISBN-13: 978-0-13-796489-5

Print Offer:  
ISBN-10: 0-13-796487-0  
ISBN-13: 978-0-13-796487-1

## To the Student

With the hope that this work will stimulate an interest in Engineering Mechanics and Mechanics of Materials and provide an acceptable guide to its understanding.

*This page intentionally left blank*

This book represents a combined abridged version of two of the author's books, namely *Engineering Mechanics: Statics, Fifteenth Edition* and *Mechanics of Materials, Eleventh Edition*. It provides a clear and thorough presentation of both the theory and application of the important fundamental topics of these subjects, that are often used in many engineering disciplines. The development emphasizes the importance of satisfying equilibrium, compatibility of deformation, and material behavior requirements. The hallmark of the book, however, remains the same as the author's unabridged versions, and that is, strong emphasis is placed on drawing a free-body diagram, and the importance of selecting an appropriate coordinate system and an associated sign convention whenever the equations of mechanics are applied. Throughout the book, many analysis and design applications are presented, which involve mechanical elements and structural members often encountered in engineering practice.

---

## New to this Edition

- **Expanded Answer Section.** The answer section in the back of the book now includes additional information related to the solution of select Fundamental Problems in order to offer the student some guidance in solving the problems.
- **Re-writing of Text Material.** Further clarification of some concepts has been included in this edition, and throughout the book the accuracy has been enhanced, and important definitions are now in boldface throughout the book to highlight their importance.
- **New Photos.** The relevance of knowing the subject matter is reflected by the real-world applications depicted in the many new or updated photos placed throughout the book. These photos generally are used to explain how the relevant principles apply to real-world situations and how materials behave under load.



- **New Problems.** There are approximately 30% new problems that have been added to this edition, which involve applications to many different fields of engineering.
- **New Videos.** Three types of videos are available that are designed to enhance the most important material in the book. Lecture videos serve to test the student's ability to understand the concepts. Example problem videos are intended to review these problems, and fundamental problem videos guide the student in solving these problems that are in the book.

---

## Hallmark Features

Besides the new features just mentioned, other outstanding features that define the contents of the text include the following.

**Organization and Approach.** Each chapter is organized into well-defined sections that contain an explanation of specific topics, illustrative example problems, and a set of homework problems. The topics within each section are placed into subgroups defined by boldface titles. The purpose of this is to present a structured method for introducing each new definition or concept and to make the book convenient for later reference and review.

**Chapter Contents.** Each chapter begins with a photo demonstrating a broad-range application of the material within the chapter. A bulleted list of the chapter contents is provided to give a general overview of the material that will be covered.

**Emphasis on Free-Body Diagrams.** Drawing a free-body diagram is particularly important when solving problems, and for this reason, this step is strongly emphasized throughout the book. In particular, within the statics coverage some sections are devoted to show how to draw free-body diagrams. Specific homework problems have also been added to develop this practice.

**Procedures for Analysis.** A general procedure for analyzing any mechanics problem is presented at the end of the first chapter. Then this procedure is customized to relate to specific types of problems that are covered throughout the book. This unique feature provides the student with a logical and orderly method to follow when applying the theory. The example problems are solved using this outlined method in order to clarify its numerical application. Realize, however, that once the relevant principles have been mastered and enough confidence and judgment have been obtained, the student can then develop his or her own procedures for solving problems.

**Important Points.** This feature provides a review or summary of the most important concepts in a section and highlights the most significant points that should be realized when applying the theory to solve problems.

**Conceptual Understanding.** Through the use of photographs placed throughout the book, the theory is applied in a simplified way in order to illustrate some of its more important conceptual features and instill the physical meaning of many of the terms used in the equations. These simplified applications increase interest in the subject matter and better prepare the student to understand the examples and solve problems.

**Fundamental Problems.** These problems may be considered as extended examples, since the key equations and answers are all listed in the back of the book. Additionally, when assigned, these problems offer students an excellent means of preparing for exams, and they can be used at a later time as a review when studying for the Fundamentals of Engineering Exam.

**Homework Problems.** Apart from the Fundamental type problems mentioned previously, other types of problems contained in the book include the following:

- **General Analysis and Design Problems.** The majority of problems in the book depict realistic situations encountered in engineering practice. Some of these problems come from actual products used in industry. It is hoped that this realism will both stimulate the student's interest in engineering mechanics and provide a means for developing the skill to reduce any such problem from its physical description to a model or symbolic representation to which the principles of mechanics may be applied.

Throughout the book, there is an approximate balance of problems using either SI or FPS units. Furthermore, in any set, an attempt has been made to arrange the problems in order of increasing difficulty, except for the end of chapter review problems, which are presented in random order. Problems that are simply indicated by a problem number have an answer given in the back of the book. However, an asterisk (\*) before every fourth problem number indicates a problem without an answer.

**Accuracy.** As with the previous editions, apart from the author, the accuracy of the text and problem solutions has been thoroughly checked in part by Kai Beng Yap, a practicing engineer, and a team of specialists at EPAM, including Georgii Kolobov, Ekaterina Radchenko, and Artur Akberov.

---

## Contents

The book is divided into two parts, and the material is covered in the traditional manner.

**Statics.** The subject of statics is presented in 6 chapters. The text begins in Chapter 1 with an introduction to mechanics and a discussion of units. The notion of a vector and the properties of a concurrent force system are introduced in Chapter 2. Chapter 3 contains a general discussion of concentrated force systems and the methods used to simplify them. The principles of rigid-body equilibrium are developed in Chapter 4

and then applied to specific problems involving the equilibrium of trusses, frames, and machines in Chapter 5. Finally, topics related to the center of gravity, centroid, and moment of inertia are treated in Chapter 6.

**Mechanics of Materials.** This portion of the text is covered in 10 chapters. Chapter 7 begins with a formal definition of both normal and shear stress, and a discussion of normal stress in axially loaded members and average shear stress caused by direct shear; finally, normal and shear strain are defined. In Chapter 8, a discussion of some of the important mechanical properties of materials is given. Separate treatments of axial load, torsion, bending, and transverse shear are presented in Chapters 9, 10, 11, and 12, respectively. Chapter 13 provides a partial review of the material covered in the previous chapters, in which the state of stress resulting from combined loadings is discussed. In Chapter 14, the concepts for transforming stress and strain are presented. Chapter 15 provides a means for a further summary and review of previous material by covering design of beams based on allowable stress. In Chapter 16, various methods for computing deflections of beams are presented, including the method for finding the reactions on these members if they are statically indeterminate. Lastly, Chapter 17 provides a discussion of column buckling.

Sections of the book that contain more advanced material are indicated by a star (\*). Time permitting, some of these topics may be included in the course. Furthermore, this material provides a suitable reference for basic principles when it is covered in other courses, and it can be used as a basis for assigning special projects.

### **Alternative Method for Coverage of Mechanics of Materials.**

It is possible to cover many of the topics in the text in several different sequences. For example, some instructors prefer to cover stress and strain transformations *first*, before discussing specific applications of axial load, torsion, bending, and shear. One possible method for doing this would be to first cover stress and strain and its transformations, Chapter 7 and Chapter 14, then Chapters 8 through 13 can be covered with no loss in continuity.

---

## Acknowledgments

Over the years, this text has been shaped by the suggestions and comments of many of my colleagues in the teaching profession. Their encouragement and willingness to provide constructive criticism are very much appreciated and it is hoped that they will accept this anonymous recognition. A note of thanks is also given to the reviewers of both my *Engineering Mechanics: Statics and Mechanics of Materials* texts. Their comments have guided the improvement of this book as well.

In particular, I would like to thank: S. Apple, A. Bazar, Fullerton, M. Hughes, R. Jackson, E. Tezak, H. Zhao,, K. Dennehy, A. Lutz, M. Walter, M. Zhang, A. Asgharatal, S. Ahmad, J. Aurand, D. Boyajian, J. Callahan, D. Dikin, I. Elishakoff, R. Hendricks, F. Herrera, J. Hilton, H. Kuhlman, K. Leipold, C. Roche, M. Rosengren, R. Scott, J. Tashbar, M. Bailey, B. Smith, and J. Nadeau.

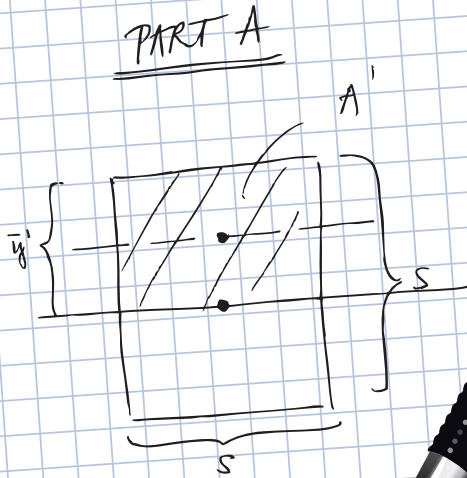
During the production process I am thankful for the assistance of Rose Kernan, my production editor for many years, and to my wife, Conny, for her help with the proofreading and typing that was needed to prepare the manuscript for publication.

A special note of thanks also goes to Jun Hwa Lee who provided a careful reading of the manuscript and also checked some of the problems. Through the years, however, Kai Beng Yap supported me in this regard, but unfortunately his support has come to an end due to his untimely passing. His contribution to this effort and his friendship will be deeply missed. Finally, I would also like to thank all my students who have used the previous edition and have made comments to improve its contents; including those in the teaching profession who have taken the time to e-mail me their comments.

I would greatly appreciate hearing from you at any time if you have any comments or suggestions regarding the contents of this edition.

*Russell Charles Hibbeler*  
*hibbeler@bellsouth.net*

# your work...



$$S = 6.75 \text{ in}$$

$$\bar{y}' = \frac{S}{2} = \frac{6.75 \text{ in}}{2} = 3.375 \text{ in}$$

$$A' = S \times 0.5 \times S = 6.75 \text{ in} \times 0.5 \times 6.75 \text{ in} = 22.8 \text{ in}^2$$

$$Q = \bar{y}' A' = 3.375 \text{ in} \times 22.8 \text{ in}^2 = 76.9 \text{ in}^3$$


$$Q = 76.9 \text{ in}^3$$

---

## With the Power of **Mastering Engineering** for **Statics and Mechanics of Materials**

Mastering™ is the teaching and learning platform that empowers every student. By combining trusted authors' content with digital tools developed to engage students and emulate the office hours experience, Mastering personalizes learning and improves results for each student.

Express your answer to three significant figures and include appropriate units.



$Q =$

**Submit**

[Hints](#) [My Answers](#) [Give Up](#) [Review Part](#)

**Incorrect; Try Again; 5 attempts remaining**

The distance between the horizontal centroidal axis of area  $A'$  and the neutral axis of the beam's cross section is half the distance between the top of the shaft and the neutral axis.

## **Empower Each Learner**

Each student learns at a different pace. Personalized learning, including optional hints and wrong-answer feedback, pinpoints the precise areas where each student needs practice, giving all students the support they need — when and where they need it — to be successful.

Learn more at [www.pearson.com/mastering/engineering](http://www.pearson.com/mastering/engineering)

---

## Mastering Engineering

This online tutorial and assessment program allows you to integrate dynamic homework and practice problems with automated grading of exercises from the textbook. Tutorials and many end-of-section problems provide enhanced student feedback and optional hints. Mastering Engineering™ allows you to easily track the performance of your entire class on an assignment-by-assignment basis, or the detailed work of an individual student. For more information visit [www.masteringengineering.com](http://www.masteringengineering.com).

---

## Resources for Instructors

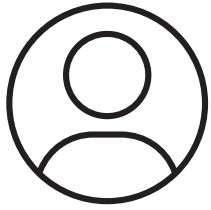
**Instructor's Solutions Manual** This supplement provides complete solutions supported by problem statements and problem figures. The Instructor's Solutions Manual is available in PDF format on Pearson Higher Education website: [www.pearson.com](http://www.pearson.com).

**PowerPoint Slides** A complete set of all the figures and tables from the textbook are available in PowerPoint format.

---

## Resources for Students

**Videos** Developed by the author, three different types of videos are now available to reinforce learning the basic theory and applying the principles. The first set provides a lecture review and a self-test of the material related to the theory and concepts presented in the book. The second set provides a self-test of the example problems and the basic procedures used for their solution. And the third set provides an engagement for solving the Fundamental Problems throughout the book. For more information on how to access these videos visit [www.pearson.com/hibbeler](http://www.pearson.com/hibbeler).



# Pearson's Commitment to Diversity, Equity, and Inclusion

**Pearson is dedicated to creating bias-free content that reflects the diversity, depth, and breadth of all learners' lived experiences.**

We embrace the many dimensions of diversity, including but not limited to race, ethnicity, gender, sex, sexual orientation, socioeconomic status, ability, age, and religious or political beliefs.

Education is a powerful force for equity and change in our world. It has the potential to deliver opportunities that improve lives and enable economic mobility. As we work with authors to create content for every product and service, we acknowledge our responsibility to demonstrate inclusivity and incorporate diverse scholarship so that everyone can achieve their potential through learning. As the world's leading learning company, we have a duty to help drive change and live up to our purpose to help more people create a better life for themselves and to create a better world.

## **Our ambition is to purposefully contribute to a world where:**

- Everyone has an equitable and lifelong opportunity to succeed through learning.
- Our educational content accurately reflects the histories and lived experiences of the learners we serve.
- Our educational products and services are inclusive and represent the rich diversity of learners.
- Our educational content prompts deeper discussions with students and motivates them to expand their own learning (and worldview).

## **Accessibility**

We are also committed to providing products that are fully accessible to all learners. As per Pearson's guidelines for accessible educational Web media, we test and retest the capabilities of our products against the highest standards for every release, following the WCAG guidelines in developing new products for copyright year 2022 and beyond.



You can learn more about Pearson's commitment to accessibility at <https://www.pearson.com/us/accessibility.html>



## **Contact Us**

While we work hard to present unbiased, fully accessible content, we want to hear from you about any concerns or needs with this Pearson product so that we can investigate and address them.



Please contact us with concerns about any potential bias at <https://www.pearson.com/report-bias.html>



For accessibility-related issues, such as using assistive technology with Pearson products, alternative text requests, or accessibility documentation, email the Pearson Disability Support team at [disability.support@pearson.com](mailto:disability.support@pearson.com)



*This page intentionally left blank*

# CONTENTS



## 1 General Principles 3

Chapter Objectives 3

- 1.1 Mechanics 3
- 1.2 Fundamental Concepts 4
- 1.3 The International System of Units 8
- 1.4 Numerical Calculations 10
- 1.5 General Procedure for Analysis 12

## 2 Force Vectors 17

Chapter Objectives 17

- 2.1 Scalars and Vectors 17
- 2.2 Vector Operations 18
- 2.3 Vector Addition of Forces 20
- 2.4 Addition of a System of Coplanar Forces 30
- 2.5 Cartesian Vectors 39
- 2.6 Addition of Cartesian Vectors 42
- 2.7 Position Vectors 49
- 2.8 Force Vector Directed Along a Line 51
- 2.9 Dot Product 58



### 3 Force System Resultants 73

Chapter Objectives 73

- 3.1 Moment of a Force—Scalar Formulation 73
- 3.2 Principle of Moments 75
- 3.3 Cross Product 83
- 3.4 Moment of a Force—Vector Formulation 86
- 3.5 Moment of a Force about a Specified Axis 96
- 3.6 Moment of a Couple 104
- 3.7 Simplification of a Force and Couple System 114
- 3.8 Further Simplification of a Force and Couple System 124
- 3.9 Reduction of a Simple Distributed Loading 134

### 4 Equilibrium of a Rigid Body 147

Chapter Objectives 147

- 4.1 Conditions for Rigid-Body Equilibrium 147
- 4.2 Free-Body Diagrams 149
- 4.3 Equations of Equilibrium 158
- 4.4 Two- and Three-Force Members 164
- 4.5 Free-Body Diagrams 173
- 4.6 Equations of Equilibrium 178
- 4.7 Characteristics of Dry Friction 186
- 4.8 Problems Involving Dry Friction 191

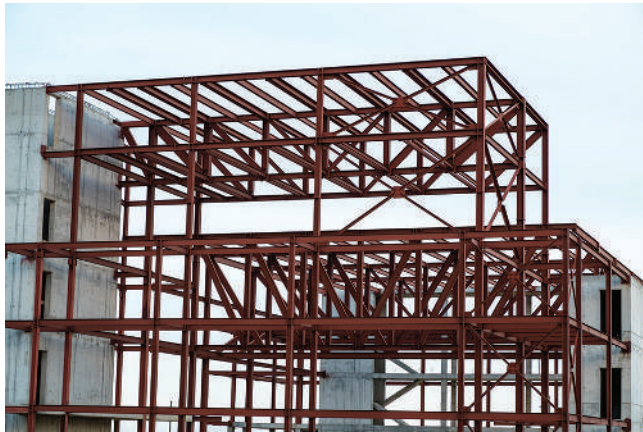




## 5 Structural Analysis 209

Chapter Objectives 209

- 5.1 Simple Trusses 209
- 5.2 The Method of Joints 212
- 5.3 Zero-Force Members 218
- 5.4 The Method of Sections 224
- 5.5 Frames and Machines 233



## 6 Center of Gravity, Centroid, and Moment of Inertia 257

Chapter Objectives 257

- 6.1 Center of Gravity and the Centroid of a Body 257
- 6.2 Composite Bodies 270
- 6.3 Moments of Inertia for Areas 278
- 6.4 Parallel-Axis Theorem for an Area 279
- 6.5 Moments of Inertia for Composite Areas 286



## 7 Stress and Strain 297

Chapter Objectives 297

- 7.1 Introduction 297
- 7.2 Internal Resultant Loadings 298
- 7.3 Stress 310
- 7.4 Average Normal Stress in an Axially Loaded Bar 312
- 7.5 Average Shear Stress 319
- 7.6 Allowable Stress Design 330
- 7.7 Deformation 345
- 7.8 Strain 346

## 8 Mechanical Properties of Materials 363

Chapter Objectives 363

- 8.1 The Tension and Compression Test 363
- 8.2 The Stress–Strain Diagram 365
- 8.3 Stress–Strain Behavior of Ductile and Brittle Materials 369
- 8.4 Strain Energy 373
- 8.5 Poisson’s Ratio 382
- 8.6 The Shear Stress–Strain Diagram 384



## 9 Axial Load 395

Chapter Objectives 395

- 9.1 Saint-Venant's Principle 395
- 9.2 Elastic Displacement of an Axially Loaded Member 397
- 9.3 Principle of Superposition 410
- 9.4 Statically Indeterminate Axially Loaded Members 410
- 9.5 The Force Method of Analysis for Axially Loaded Members 417
- 9.6 Thermal Stress 423
- 9.7 Stress Concentrations 430



## 10 Torsion 439

Chapter Objectives 439

- 10.1 Torsional Deformation of a Circular Shaft 439
- 10.2 The Torsion Formula 442
- 10.3 Power Transmission 450
- 10.4 Angle of Twist 460
- 10.5 Statically Indeterminate Torque-Loaded Members 474
- \*10.6 Solid Noncircular Shafts 481
- 10.7 Stress Concentration 484



## 11 Bending 495

- Chapter Objectives 495
- 11.1 Internal Loading as a Function of Position 495
- 11.2 Graphical Method for Constructing Shear and Moment Diagrams 502
- 11.3 Bending Deformation of a Straight Member 519
- 11.4 The Flexure Formula 523
- 11.5 Unsymmetric Bending 536
- 11.6 Stress Concentrations 544

## 12 Transverse Shear 553

- Chapter Objectives 553
- 12.1 Shear in Straight Members 553
- 12.2 The Shear Formula 554
- 12.3 Shear Flow in Built-Up Members 570



## 13 Combined Loadings 583

Chapter Objectives 583

- 13.1 Thin-Walled Pressure Vessels 583
- 13.2 State of Stress Caused by Combined Loadings 590

## 14 Stress and Strain Transformation 611

Chapter Objectives 611

- 14.1 Plane-Stress Transformation 611
- 14.2 General Equations of Plane Stress Transformation 616
- 14.3 Principal Stresses and Maximum In-Plane Shear Stress 619
- 14.4 Mohr's Circle—Plane Stress 631
- 14.5 Absolute Maximum Shear Stress 642
- 14.6 Plane Strain 647
- 14.7 General Equations of Plane-Strain Transformation 648
- 14.8 Mohr's Circle—Plane Strain 656
- \*14.9 Absolute Maximum Shear Strain 663
- 14.10 Strain Rosettes 665
- 14.11 Material Property Relationships 669





## 15 Design of Beams and Shafts 687

Chapter Objectives 687

15.1 Basis for Beam Design 687

15.2 Prismatic Beam Design 690



## 16 Deflection of Beams and Shafts 705

Chapter Objectives 705

16.1 The Elastic Curve 705

16.2 Slope and Displacement by  
Integration 709

\* 16.3 Discontinuity Functions 725

16.4 Method of Superposition 736

16.5 Statically Indeterminate Beams and  
Shafts—Method of Superposition 744



## 17

### Buckling of Columns 761

- Chapter Objectives 761
- 17.1 Critical Load 761
- 17.2 Ideal Column with Pin Supports 764
- 17.3 Columns Having Various Types of Supports 770
- \*17.4 The Secant Formula 780

## Appendix

- A. Mathematical Review and Expressions 792
- B. Geometric Properties of an Area and Volume 796
- C. Geometric Properties of Wide-Flange Sections 798
- D. Slopes and Deflections of Beams 802

## Fundamental Problem Solutions 804

## Answers to Selected Problems 839

## Index 853

*This page intentionally left blank*

# CREDITS

**Cover:** Jess Kraft/Shutterstock

## Chapter 1:

**2 ALAMY IMAGES:** Gaertner/Alamy Stock Photo

**6 SHUTTERSTOCK:** NikoNomad/Shutterstock

## Chapter 2:

**16 ALAMY IMAGES:** Marcus Hofmann/Alamy Stock Photo

## Chapter 3:

**72 SHUTTERSTOCK:** Zbynek Jirousek/Shutterstock

## Chapter 4:

**146 ALAMY IMAGES:** Stephan Scherhag/Panther Media GmbH/Alamy Stock Photo

## Chapter 5:

**208 ALAMY IMAGES:** Ray Hardinge/Alamy Stock Photo

## Chapter 6:

**256 ALAMY IMAGES:** Olaf Speier/Alamy Stock Photo

## Chapter 7:

**296 SHUTTERSTOCK:** Ilya Akinshin/Shutterstock

## Chapter 8:

**362 123RF GB LIMITED:** John Vlahidis/123RF

## Chapter 9:

**394 SHUTTERSTOCK:** BalLi8Tic/Shutterstock

## Chapter 10:

**438 SHUTTERSTOCK:** Vadim Ratnikov/Shutterstock

## Chapter 11:

**494 123RF GB LIMITED:** Aydo8/123RF

## Chapter 12:

**552 123RF GB LIMITED:** Claudiodivizia/123RF

**Chapter 13:****582 123RF GB LIMITED:** Ganna Poltoratska/123RF**Chapter 14:****610 SHUTTERSTOCK:** ID1974/Shutterstock**Chapter 15:****686 SHUTTERSTOCK:** Sasin Paraksa/Shutterstock**Chapter 16:****704 SHUTTERSTOCK:** Lev Kropotov/Shutterstock**Chapter 17:****760 SHUTTERSTOCK:** Ann Baldwin/Shutterstock

# STATICS AND MECHANICS OF MATERIALS

SIXTH EDITION

# CHAPTER 1



Cranes such as this one are required to lift extremely large loads. Their design is based on the basic principles of statics and dynamics, which form the subject matter of engineering mechanics.

# GENERAL PRINCIPLES

## CHAPTER OBJECTIVES

---

- To provide an introduction to the basic quantities and idealizations of mechanics.
  - To state Newton's Laws of Motion.
  - To review the principles for applying the SI system of units.
  - To examine the standard procedures for performing numerical calculations.
  - To present a general guide for solving problems.
- 

## 1.1 MECHANICS

**Mechanics** can be defined as that branch of the physical sciences concerned with the state of rest or motion of bodies that are subjected to the action of forces. In this book we will study two important branches of mechanics, namely, statics and mechanics of materials. These subjects form a suitable basis for the design and analysis of many types of structural, mechanical, or electrical devices encountered in engineering.

**Statics** deals with the equilibrium of bodies, that is, it is used to determine the forces acting either external to the body or within it that are necessary to keep the body in equilibrium. *Mechanics of materials* studies the relationships between the external loads and the distribution of internal forces acting within the body. This subject is also concerned with finding the deformations of the body, and it provides a study of the body's stability.



In this book we will first study the principles of statics, since for the design and analysis of any structural or mechanical element it is *first* necessary to determine the forces acting both on and within its various members. Once these internal forces are determined, the size of the members, their deflection, and their stability can then be determined using the fundamentals of mechanics of materials, which will be covered later.

**Historical Development.** The subject of statics developed very early in history because its principles can be formulated simply from measurements of geometry and force. For example, the writings of Archimedes (287–212 B.C.) deal with the principle of the lever. Studies of the pulley and inclined plane are also recorded in ancient writings—at times when the requirements for engineering were limited primarily to building construction.

The origin of mechanics of materials dates back to the beginning of the seventeenth century, when Galileo performed experiments to study the effects of loads on rods and beams made of various materials. However, at the beginning of the eighteenth century, experimental methods for testing materials were vastly improved, and at that time many experimental and theoretical studies in this subject were undertaken primarily in France, by such notables as Saint-Venant, Poisson, Lamé, and Navier.

Over the years, after many of the fundamental problems of mechanics of materials had been solved, it became necessary to use advanced mathematical and computer techniques to solve more complex problems. As a result, this subject has expanded into other areas of mechanics, such as the *theory of elasticity* and the *theory of plasticity*. Research in these fields is ongoing, in order to meet the demands for solving more advanced problems in engineering.

## 1.2 FUNDAMENTAL CONCEPTS

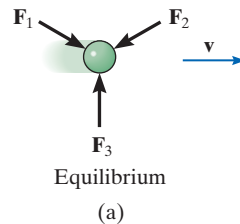
Before we begin our study, it is important to understand the definitions of certain fundamental concepts and principles.

**Mass.** *Mass* is a measure of a *quantity of matter* that is used to compare the action of one body with that of another. This property provides a measure of the resistance of matter to a change in velocity.

**Force.** In general, *force* is considered as a “push” or “pull” exerted by one body on another. This interaction can occur when there is direct contact between the bodies, such as a person pushing on a wall, or it can occur through a distance when the bodies are physically separated. Examples of the latter type include gravitational, electrical, and magnetic forces. In any case, a force is completely characterized by its magnitude, direction, and point of application.

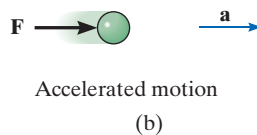
**Newton's Three Laws of Motion.** Engineering mechanics is formulated on the basis of Newton's three laws of motion, the validity of which is based on experimental observation. These laws apply to the motion of a particle as measured from a *nonaccelerating* reference frame. They may be briefly stated as follows.

**First Law.** A particle originally at rest, or moving in a straight line with constant velocity, tends to remain in this equilibrium state provided the particle is *not* subjected to an unbalanced force, Fig. 1-1*a*.

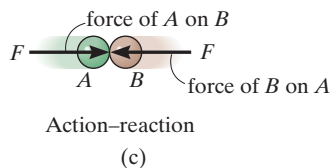


**Second Law.** A particle acted upon by an *unbalanced force*  $\mathbf{F}$  experiences an acceleration  $\mathbf{a}$  that has the same direction as the force and a magnitude that is directly proportional to the force, Fig. 1-1*b*.<sup>\*</sup> If the particle has a mass  $m$ , this law may be expressed mathematically as

$$\mathbf{F} = m\mathbf{a} \quad (1-1)$$



**Third Law.** The mutual forces of action and reaction between two particles are equal, opposite, and collinear, Fig. 1-1*c*.



**Fig. 1-1**

<sup>\*</sup>Stated another way, the unbalanced force acting on the particle is proportional to the time rate of change of the particle's linear momentum.

**Newton's Law of Gravitational Attraction.** Shortly after formulating his three laws of motion, Newton postulated a law governing the gravitational attraction between any two particles. Stated mathematically,

$$F = G \frac{m_1 m_2}{r^2} \quad (1-2)$$

where

$F$  = force of gravitation between the two particles

$G$  = universal constant of gravitation; according to experimental evidence,  $G = 66.73(10^{-12}) \text{ m}^3/(\text{kg} \cdot \text{s}^2)$

$m_1, m_2$  = mass of each of the two particles

$r$  = distance between the two particles



The astronaut's weight is diminished since she is far removed from the gravitational field of the earth.

**Weight.** According to Eq. 1-2, any two particles or bodies have a mutual attractive (gravitational) force acting between them. In the case of a particle located at or near the surface of the earth, however, the only gravitational force having any sizable magnitude is that between the earth, because of its very large mass, and the particle. Consequently, this force, called the *weight*, will be the only gravitational force we will consider.

From Eq. 1-2, if the particle has a mass  $m_1 = m$ , and we assume the earth is a nonrotating sphere of constant density and having a mass  $m_2 = M_e$ , then if  $r$  is the distance between the earth's center and the particle, the weight  $W$  of the particle becomes

$$W = G \frac{mM_e}{r^2}$$

If we let  $g = GM_e/r^2$ , we have

$$W = mg \quad (1-3)$$

If we allow the particle to fall downward, then neglecting air resistance, the only force acting on the particle is its weight, and so Eq. 1-1 becomes  $W = ma$ . Comparing this result with Eq. 1-3, we see that  $a = g$ . In other words,  $g$  is the acceleration due to gravity. Since it depends on  $r$ , then the weight of the particle or body is *not* an absolute quantity. Instead, its magnitude depends upon the elevation where the measurement was made. For most engineering calculations, however,  $g$  is determined at sea level and at a latitude of  $45^\circ$ , which is considered the "standard location."

**Idealizations.** Models or idealizations are used in mechanics in order to simplify application of the theory. Here we will consider three important idealizations.

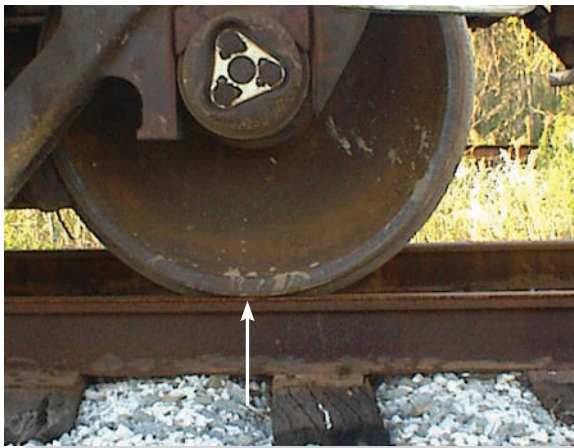
**Particle.** A *particle* has a mass, but a size that can be neglected. For example, the size of the earth is insignificant compared to the size of its orbit, and therefore the earth can be modeled as a particle when studying its orbital motion. When a body is idealized as a particle, the principles of mechanics reduce to a rather simplified form since the geometry of the body *will not be involved* in the analysis of the problem.

**Rigid Body.** A *rigid body* can be considered as a combination of a large number of particles in which all the particles remain at a fixed distance from one another, both before and after applying a load. This model is important because the body's shape does not change when a load is applied, and so we do not have to consider the type of material from which the body is made. In most cases the actual deformations occurring in structures, machines, mechanisms, and the like are relatively small, and the rigid-body assumption is suitable for analysis.

**Concentrated Force.** A *concentrated force* represents the effect of a loading which is assumed to act at a point on a body. We can represent a load by a concentrated force, provided the area over which the load is applied is very small compared to the overall size of the body. An example would be the contact force between a wheel and the ground.



Three forces act on the ring. Since these forces all meet at a point, then for any force analysis, we can assume the ring to be represented as a particle.



Steel is a common engineering material that does not deform very much under load. Therefore, we can consider this railroad wheel to be a rigid body acted upon by the concentrated force of the rail.

TABLE 1–1 SI System of Units

Name	Length	Time	Mass	Force
International System of Units	meter	second	kilogram	newton*
SI	m	s	kg	N $\left(\frac{\text{kg}\cdot\text{m}}{\text{s}^2}\right)$

\*Derived unit.

## 1.3 THE INTERNATIONAL SYSTEM OF UNITS

The four basic quantities—length, time, mass, and force—are not all independent from one another; in fact, they are *related* by Newton’s second law of motion,  $\mathbf{F} = m\mathbf{a}$ . Because of this, the *units* used to measure these quantities cannot *all* be selected arbitrarily. The equality  $\mathbf{F} = m\mathbf{a}$  is maintained only if three of the four units, called **base units**, are *defined* and the fourth unit is then *derived* from the equation.

For the International System of Units, abbreviated SI after the French “Système International d’Unités,” length is in meters (m), time is in seconds (s), and mass is in kilograms (kg), Table 1–1. The unit of force, called a **newton** (N), is *derived* from  $\mathbf{F} = m\mathbf{a}$ . Thus, 1 newton is equal to a force required to give 1 kilogram of mass an acceleration of  $1 \text{ m/s}^2$  ( $\text{N} = \text{kg}\cdot\text{m/s}^2$ ).

If the weight of a body located at the “standard location” is to be determined in newtons, then Eq. 1–3 must be applied. Here measurements give  $g = 9.80665 \text{ m/s}^2$ ; however, for calculations the value  $g = 9.81 \text{ m/s}^2$  will be used. Thus,

$$W = mg \quad (g = 9.81 \text{ m/s}^2) \quad (1-4)$$

Therefore, a body of mass 1 kg has a weight of 9.81 N, a 2-kg body weighs 19.62 N, and so on, Fig. 1–1. Perhaps it is easier to remember that a small apple weighs one newton. Also, by comparison with the U.S. Customary system of units (FPS),

$$\begin{aligned} 1 \text{ pound (lb)} &= 4.448 \text{ N} \\ 1 \text{ foot (ft)} &= 0.3048 \text{ m} \end{aligned}$$

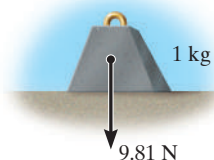


Fig. 1–1

**Prefixes.** When a numerical quantity is either very large or very small, the units used to define its size may be modified by using a prefix. Some of the prefixes used in the SI system are shown in Table 1–2. Each represents a multiple or submultiple of a unit which, if applied successively, moves

the decimal point of a numerical quantity to every third place.\* For example, 4 000 000 N = 4 000 kN (kilo-newton) = 4 MN (mega-newton), or 0.005 m = 5 mm (milli-meter). Notice that the SI system does not include the multiple deca (10) or the submultiple centi (0.01), which form part of the metric system. Except for some volume and area measurements, the use of these prefixes is generally avoided in science and engineering.

TABLE 1–2 Prefixes

	Exponential Form	Prefix	SI Symbol
<i>Multiple</i>			
1 000 000 000	$10^9$	giga	G
1 000 000	$10^6$	mega	M
1 000	$10^3$	kilo	k
<i>Submultiple</i>			
0.001	$10^{-3}$	milli	m
0.000 001	$10^{-6}$	micro	$\mu$
0.000 000 001	$10^{-9}$	nano	n

**Rules for Use.** Here are a few of the important rules that describe the proper use of the various SI symbols:

- Quantities defined by several units which are multiples of one another are separated by a *dot* to avoid confusion with prefix notation, as indicated by  $N = \text{kg} \cdot \text{m}/\text{s}^2 = \text{kg} \cdot \text{m} \cdot \text{s}^{-2}$ . Also,  $\text{m} \cdot \text{s}$  (meter-second), whereas ms (milli-second).
- The exponential power on a unit having a prefix refers to both the unit *and* its prefix. For example,  $\mu\text{N}^2 = (\mu\text{N})^2 = \mu\text{N} \cdot \mu\text{N}$ . Likewise,  $\text{mm}^2$  represents  $(\text{mm})^2 = \text{mm} \cdot \text{mm}$ .
- With the exception of the base unit the kilogram, in general avoid the use of a prefix in the denominator of composite units. For example, do not write N/mm, but rather kN/m; also, m/mg should be written as Mm/kg.
- When performing calculations, represent the numbers in terms of their *base or derived units* by converting all prefixes to powers of 10. The final result should then be expressed using a *single prefix*. Also, after calculation, it is best to keep numerical values between 0.1 and 1000; otherwise, a suitable prefix should be chosen. For example,

$$\begin{aligned} (50 \text{ kN})(60 \text{ mm}) &= [50(10^3) \text{ N}][60(10^{-9}) \text{ m}] \\ &= 3000(10^{-6}) \text{ N} \cdot \text{m} = 3(10^{-3}) \text{ N} \cdot \text{m} = 3 \text{ mN} \cdot \text{m} \end{aligned}$$

\*The kilogram is the only base unit that is defined with a prefix.